

DURABLES AND SIZE-DEPENDENCE IN THE MARGINAL PROPENSITY TO SPEND

Martin Beraja (MIT & NBER)

Nathan Zorzi (Dartmouth)

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We know little about the effectiveness of stimulus checks as they become larger
\$2,000 could be barely more effective than \$300 if households spend less and less of each additional dollar

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- ▶ Relevant quantity for policy: **total** spending, including **durables** (large share of MPX)
- ▶ Conjecture: HH might **tilt spending towards durables** for large checks (Parker et al.)

This could dampen / reverse decline in MPX predicted by models of non-durables

Build a rich and flexible model → micro data → size-dependence? checks?

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Lumpy durables

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1. Smooth hazard is key to explain a **rich set of micro facts** that existing models miss.

Discipline the shape of this hazard by matching: (i) relative MPX on durables; (ii) short-run price elasticity of durables; (iii) distribution of adjustments sizes; (iv) conditional probability of adjustment, etc.

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2. Quantify the **size-dependence** in the MPX. The **MPX declines, albeit slowly**.

MPX is flatter in purely state-dependent model of durables, declines faster in 2A model of non-durables

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A large check of \$2,000 increases output by 27 c/\$, compared to 41 c/\$ for a small check of \$300

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Larger checks remain effective, but extrapolating from small checks overestimates their impact

A Model with a Smooth Hazard

Bringing the Model to the Data

Size-Dependence in the MPX

Stimulus Checks in General Equilibrium

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where

$$u(c, d) = \frac{1}{1-\sigma} U(c, d)^{1-\sigma} \quad \text{with} \quad U(c, d) = \left[\vartheta_c^{\frac{1}{\nu}} c^{\frac{\nu-1}{\nu}} + \vartheta_d^{\frac{1}{\nu}} d^{\frac{\nu-1}{\nu}} \right]^{\frac{\nu}{\nu-1}}$$

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$$V_t(\mathbf{x}) = \max \left\{ V_t^{\text{non}}(\mathbf{x}), V_t^{\text{adjust}}(\mathbf{x}) - \kappa \right\},$$

where $\kappa > 0$ is the (utility) cost of adjustment.

- ▶ Canonical model of durables: Discontinuous hazard,

$$\mathcal{S}_t(\mathbf{x}) = \begin{cases} 1 & \text{if } V_t^{\text{adjust}}(\mathbf{x}) - \kappa > V_t^{\text{non}}(\mathbf{x}), \\ 0 & \text{otherwise} \end{cases},$$

i.e., (s, S) adjustment bands.

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- ▶ Nest two polar cases: fully **state-dependent** ($\eta \rightarrow 0$) and **time-dependent** ($\eta \rightarrow +\infty$)

Figure 1: Adjustment hazard (fixing d and y)

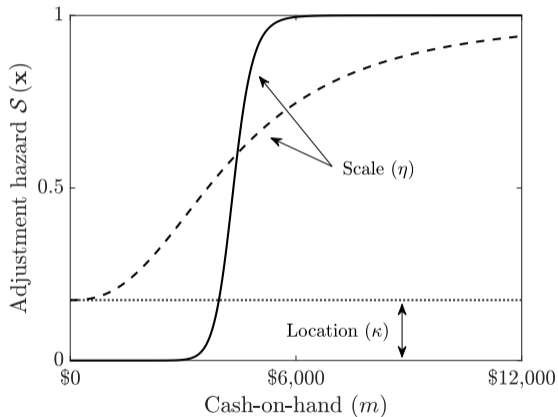
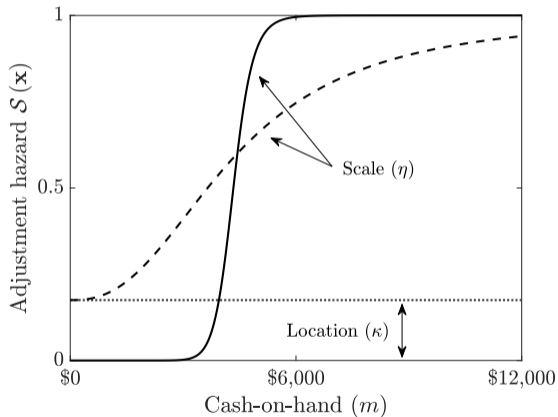


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- The shape of the **adjustment hazard** is key for the **size-dependence** in MPX

ADJUSTMENT HAZARD AND SIZE-DEPENDENCE

- ▶ Marginal propensity to spend on durables:

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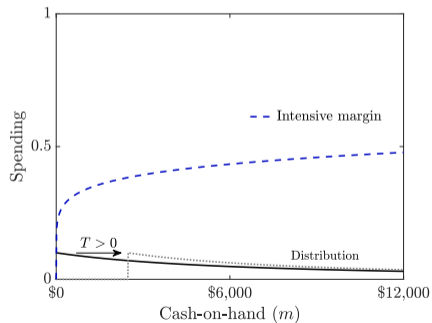
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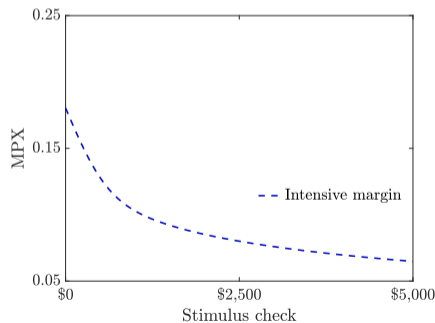
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Spending functions (fixing d)



MPX

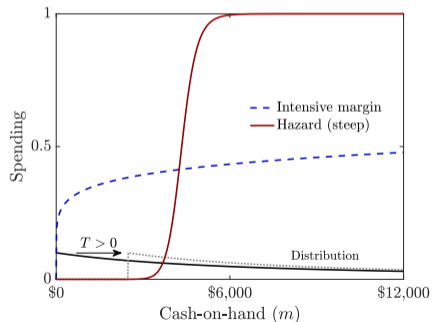


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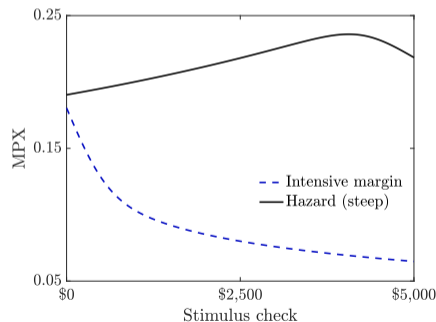
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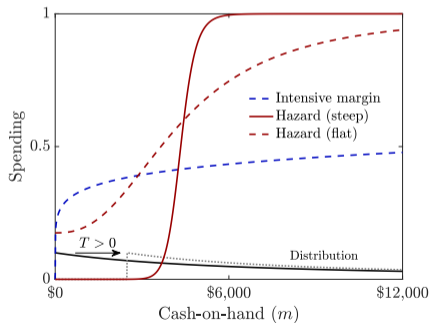


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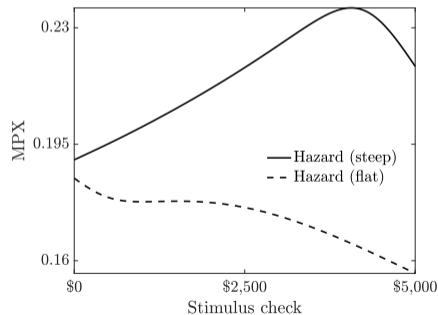
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Spending functions (fixing d)



MPX (fixing d)

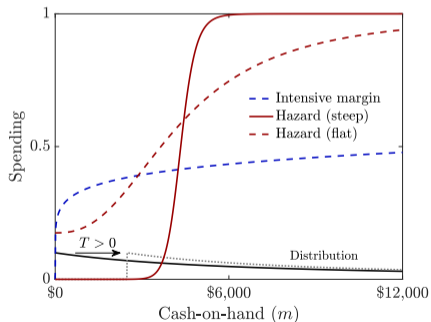


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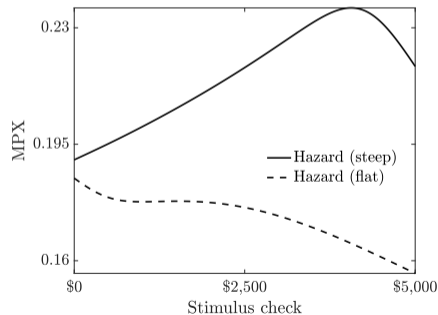
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Spending functions (fixing d)



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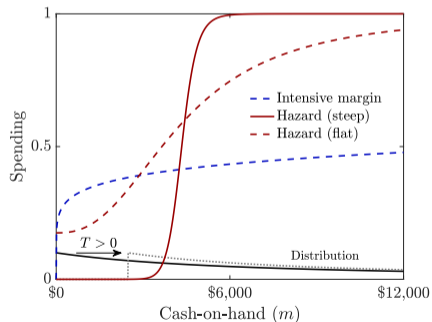
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ADJUSTMENT HAZARD AND SIZE-DEPENDENCE

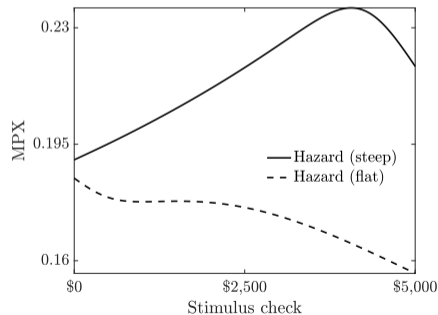
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Spending functions (fixing d)



MPX (fixing d)



- ▶ Getting the **shape of hazard** right is crucial for **size-dependence + match data**

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Parameter	Description	Calibr.	Target	Value	Source
β	Discount factor	0.944	Liquid assets / A GDP	26%	Kaplan et al.
ϑ	Non-durable parameter	0.637	Durables / non-durables	26%	CEX
ι	Maintenance	0.257	Maintenance / new investment	32.6%	CEX
κ	Location parameter	0.803	Frequency of adjustment (A)	23.8%	PSID
η	Scale parameter	0.20	Next slide		

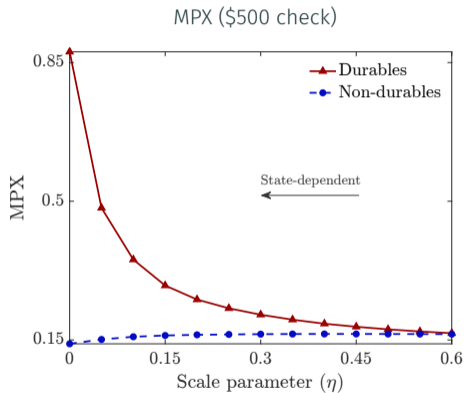
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SCALE PARAMETER (η)

- ▶ Two moments are informative: MPX out of \$500 (PE) and user cost elasticity (GE)

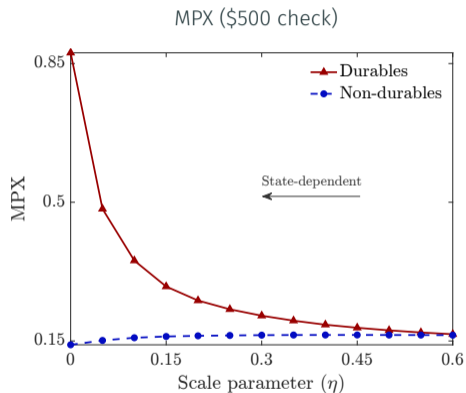
- ▶ Capture: (i) relative importance of durables; and (ii) strength of extensive margin.

SCALE PARAMETER (η)



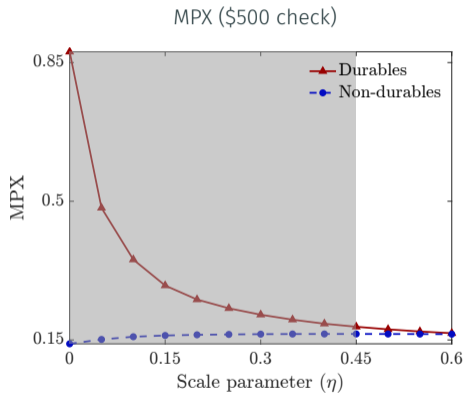
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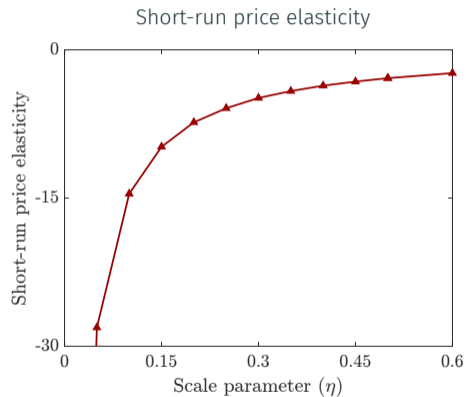
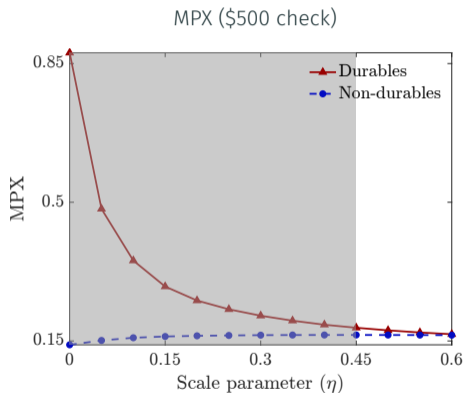
- Evidence: $MPX^d > MPX^c$ (Havranek-Sokolova) \rightarrow not too time-dependent

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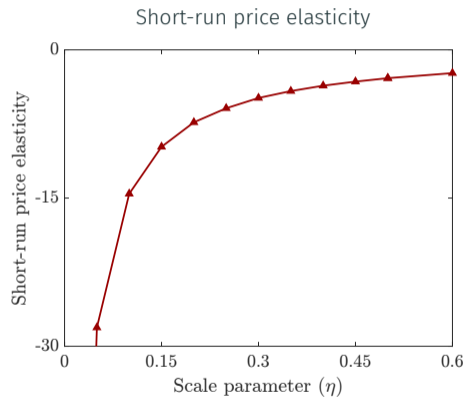
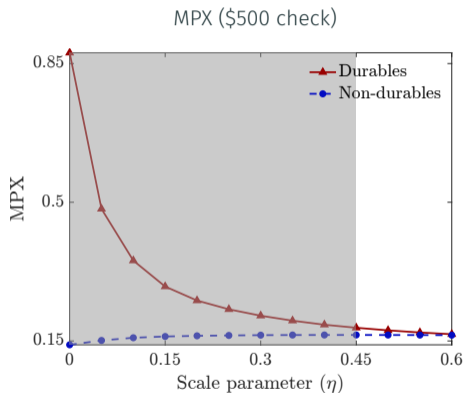
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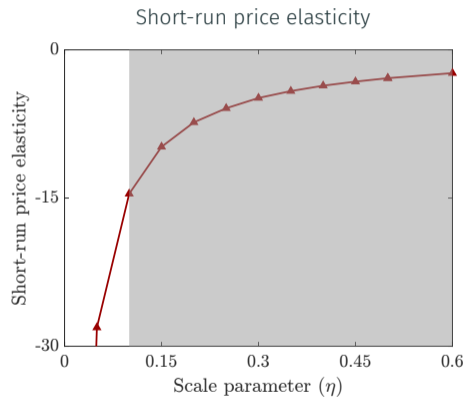
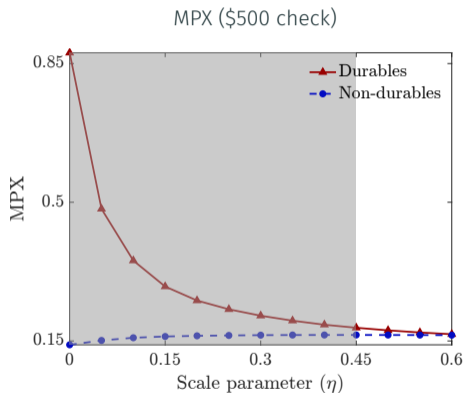
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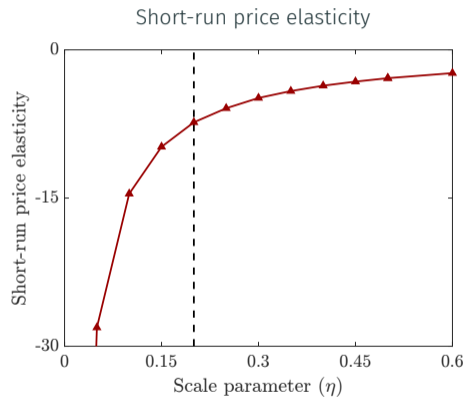
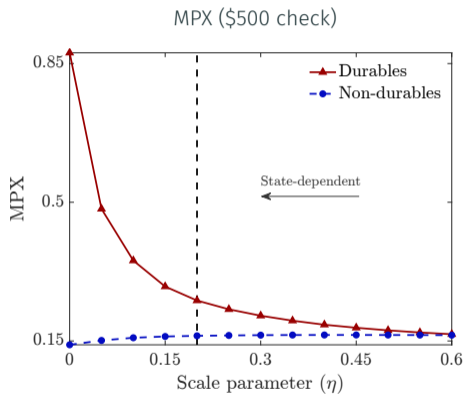
- Evidence: Elasticity ≥ -15 (Bachmann et al.) \rightarrow not too state-dependent (McKay-Wieland)

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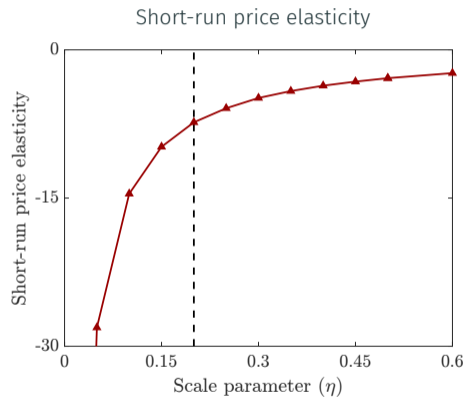
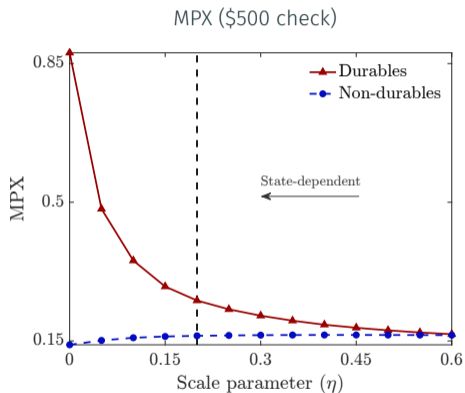
- Evidence: Elasticity ≥ -15 (Bachmann et al.) \rightarrow not too state-dependent (McKay-Wieland)

SCALE PARAMETER (η)



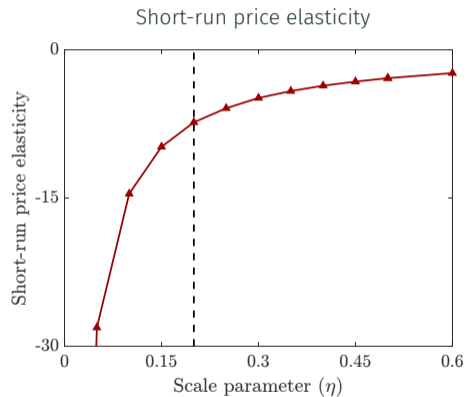
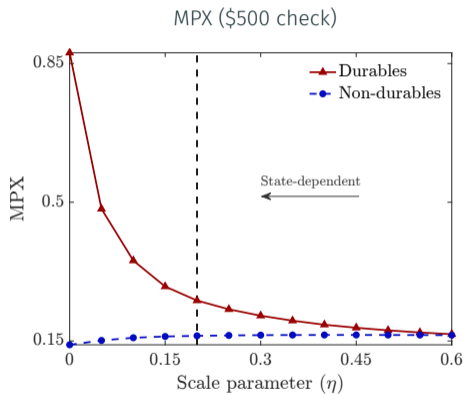
- Benchmark calibration: $\eta = 0.2$ (+ robustness checks)

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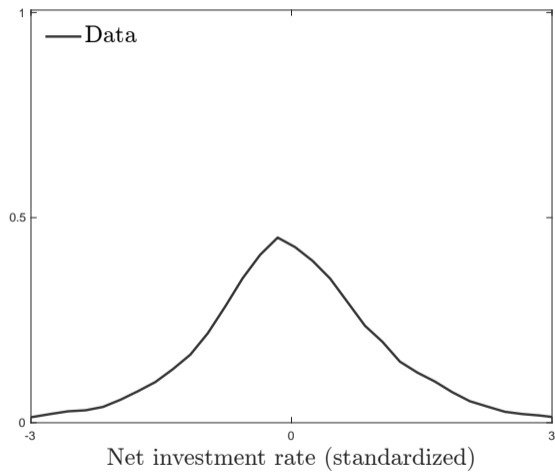
- Benchmark calibration: $MPX^d \sim 1.5 \times MPX^c$ (Havranek-Sokolova) and elasticity ~ -7

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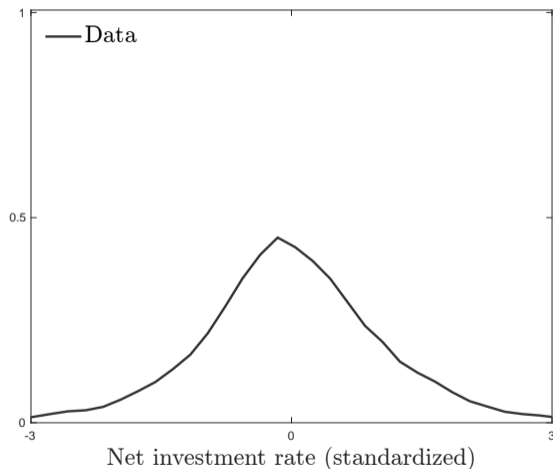


- Benchmark calibration: matches well **untargeted** moments

1. DISTRIBUTION OF ADJUSTMENTS (PSID)

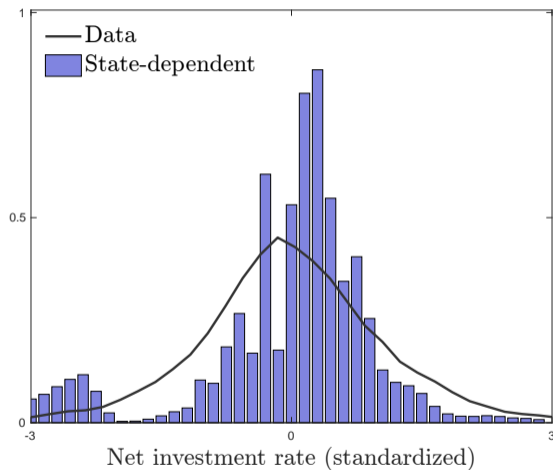


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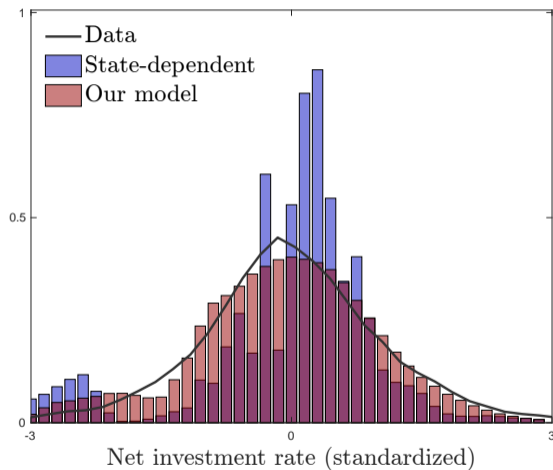
- Reflects the **shape of hazard**: $\int_{-\infty}^z f(s) ds = \int \mathbf{1}_{\{\log(d'(\mathbf{x})/d) \in (-\infty, z]\}} \mathcal{S}(\mathbf{x}) \mu(d\mathbf{x})$

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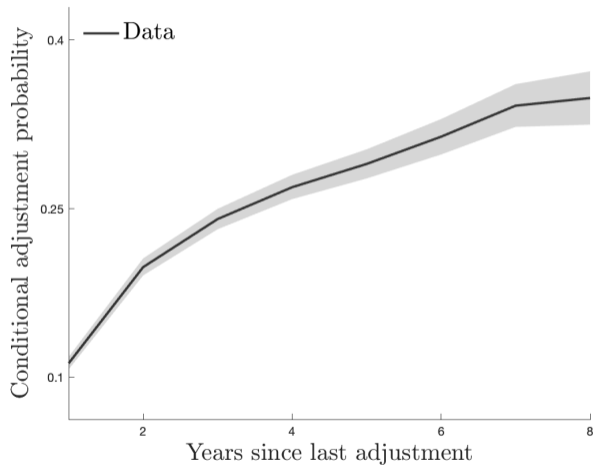
- ▶ State-dependent model: misses the overall shape, the tails, etc.

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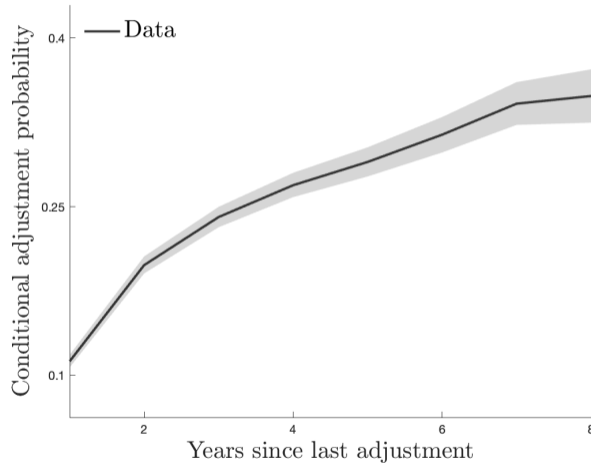
- Our model: fits the distribution closely, i.e., the data supports our smooth hazard.

2. PROBABILITY OF ADJUSTMENT SINCE LAST PURCHASE (PSID)



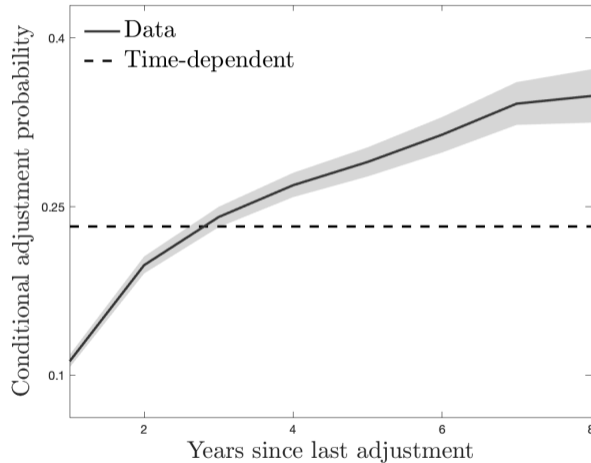
- Adjustment probability conditional on not having adjusted so far (Kaplan-Meier)

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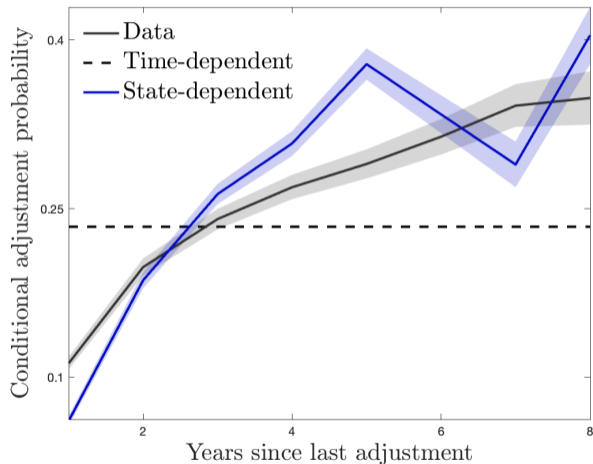
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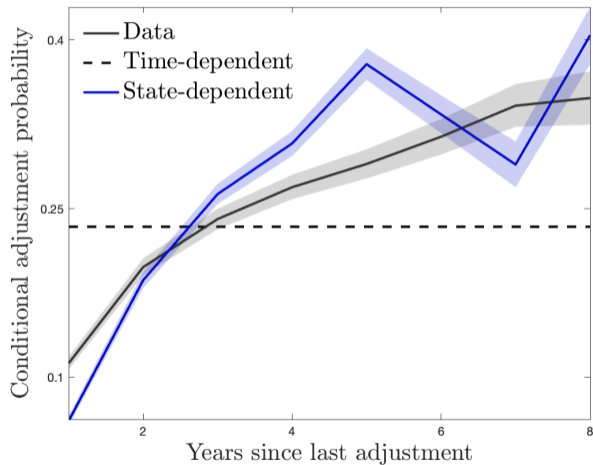
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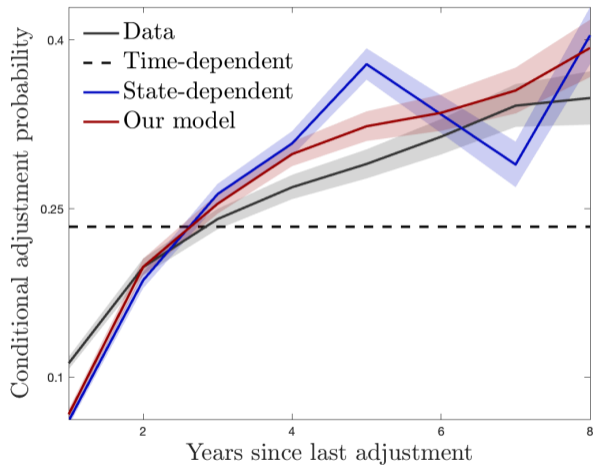
- Model-generated data discretized in PSID waves, CI are bootstrapped at 90%

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- Again, the evidence rejects the purely state- and time-dependent models.

2. PROBABILITY OF ADJUSTMENT SINCE LAST PURCHASE (PSID)



- Our model has both state-dependent and time-dependent features

3. OTHER UNTARGETED MOMENTS

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► Dynamics

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► State-dependence

► CalvoPlus

A Model with a Smooth Hazard

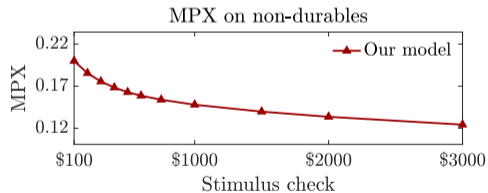
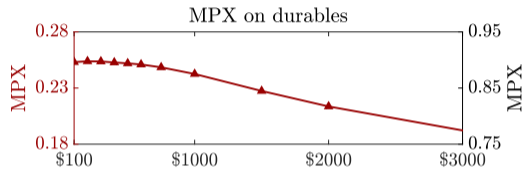
Bringing the Model to the Data

Size-Dependence in the MPX

Stimulus Checks in General Equilibrium

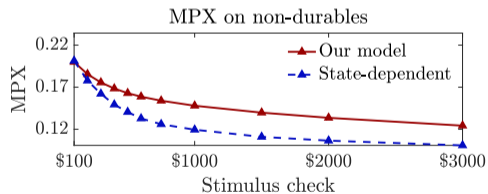
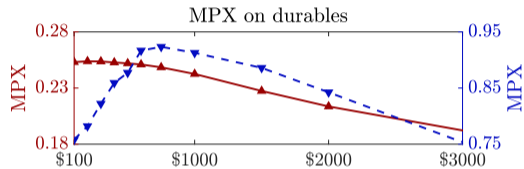
SIZE-DEPENDENCE IN THE MPX

MPX on durables and non-durables

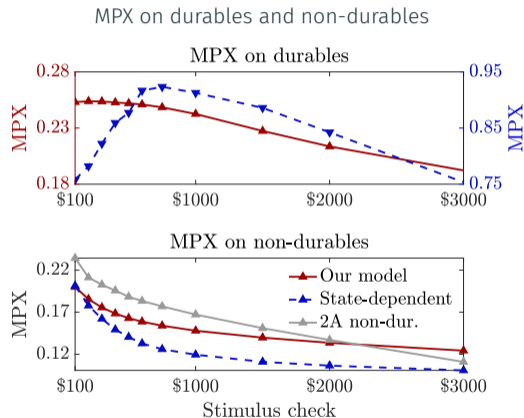


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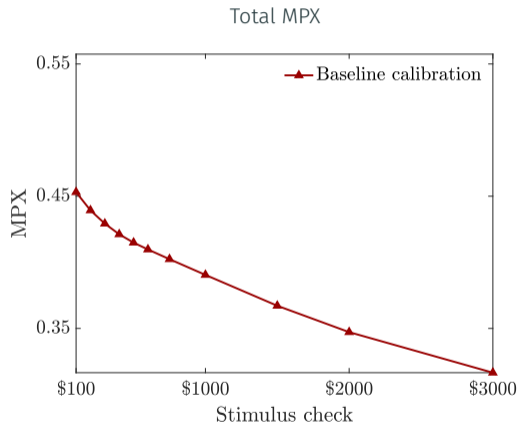
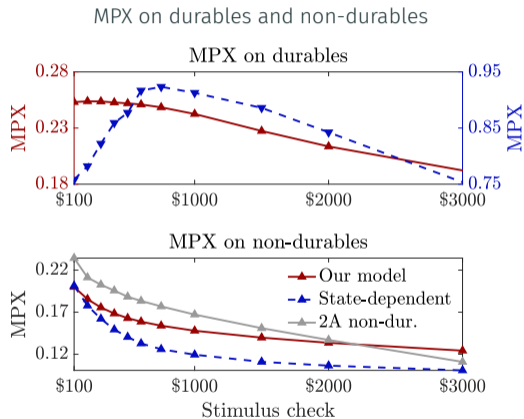


SIZE-DEPENDENCE IN THE MPX



- ▶ Modelling **durables** is important for the **MPX on non-durables** (complementarity)

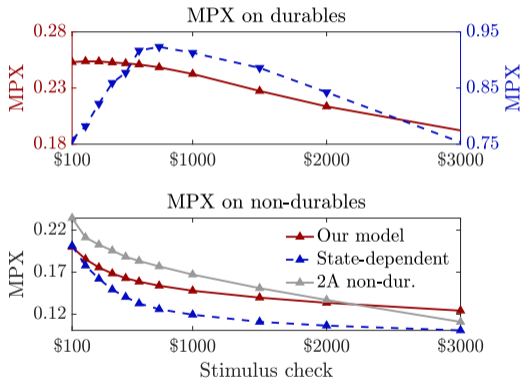
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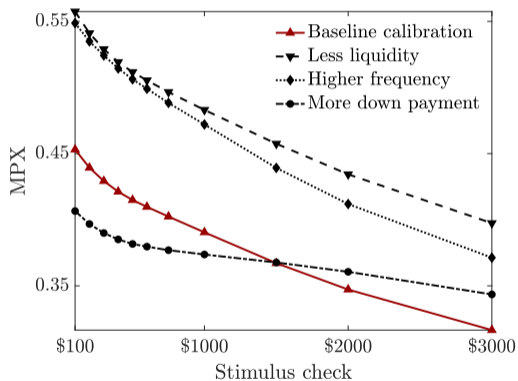
- Our model: **realistic total MPX** (level) that **decreases slowly** (size-dependence)

SIZE-DEPENDENCE IN THE MPX

MPX on durables and non-durables



Total MPX

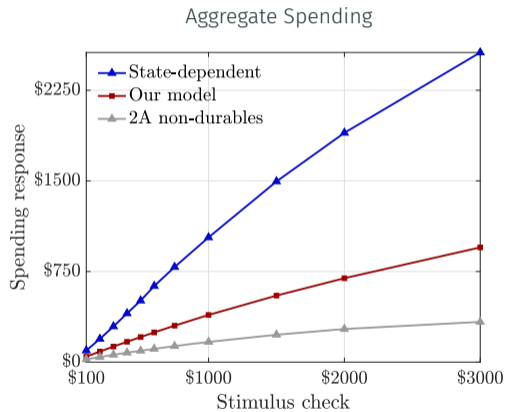


► More results:

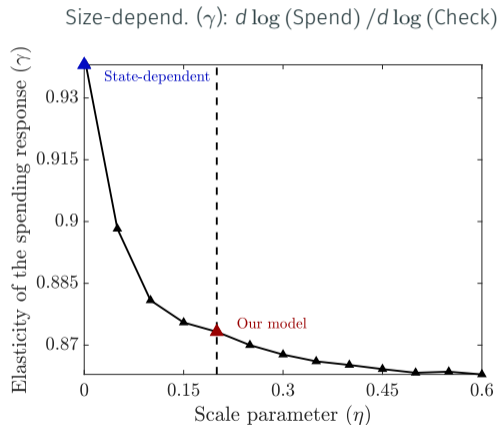
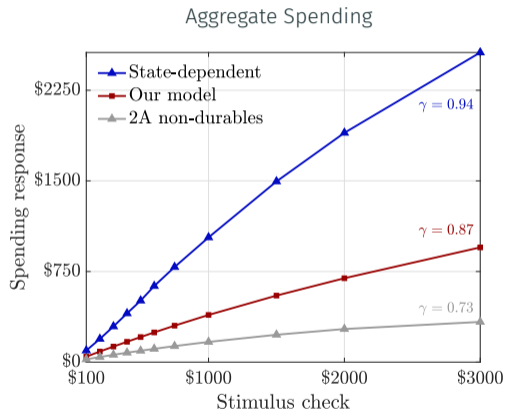
► Decomposition

► Sensitivity

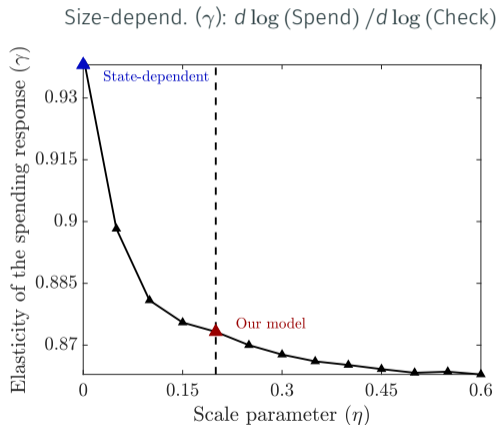
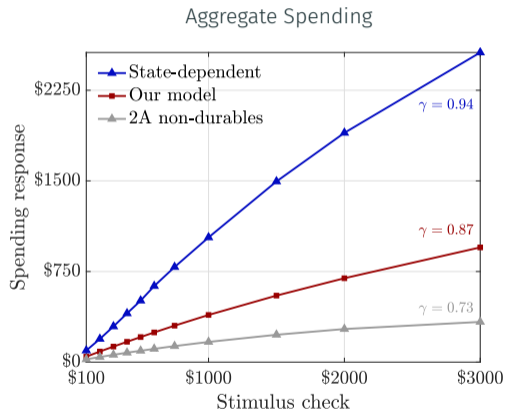
AGGREGATE SPENDING, CONCAVITY, AND THE ROLE OF η



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► The size-dependence (concavity) is very constant around $\eta = 0.2$

► State-contingency

A Model with a Smooth Hazard

Bringing the Model to the Data

Size-Dependence in the MPX

Stimulus Checks in General Equilibrium

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Imports account for 1/4 of durable spending

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- ▶ **Focus:** demand-driven recessions (2001, Great Recession)
Labor markets are slack
- ▶ An extension with **supply-side constraints** (Orchard et al., Comin et al.)
Shocks to potential output, non-linear NKPC, and relative price movements

Aggregate demand

1. Eligible for checks if $e \leq \$75,000$

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$$K_t = \{1 - \delta^K + \Phi(I_t/K_{t-1}) + z_t\} K_{t-1} \quad \longleftarrow \quad \text{Solve for } \{z_t\} \text{ that generate recession}$$

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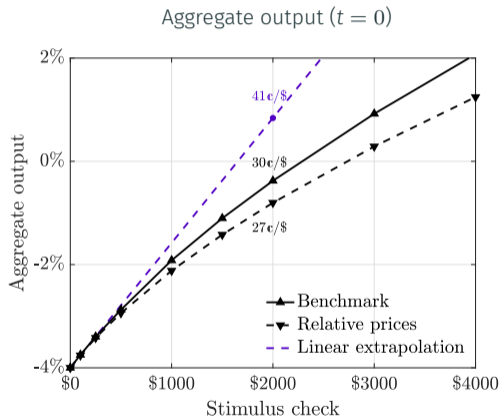
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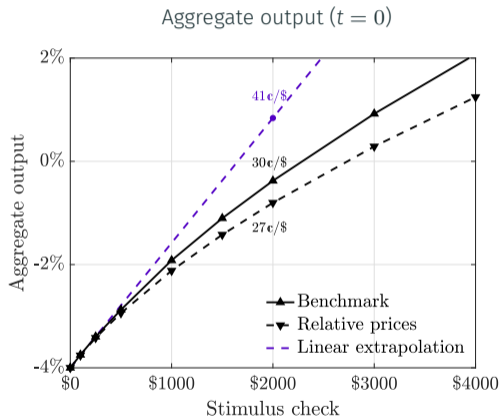
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► Closing the model

GENERAL EQUILIBRIUM RESPONSE TO STIMULUS CHECKS

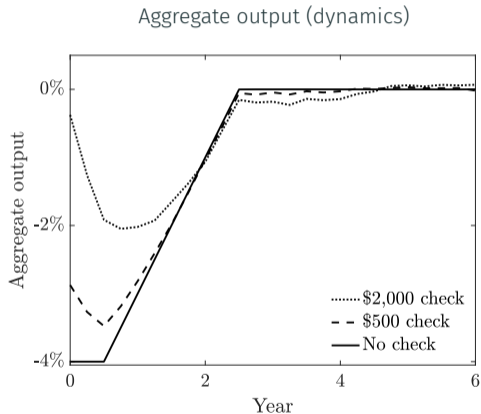
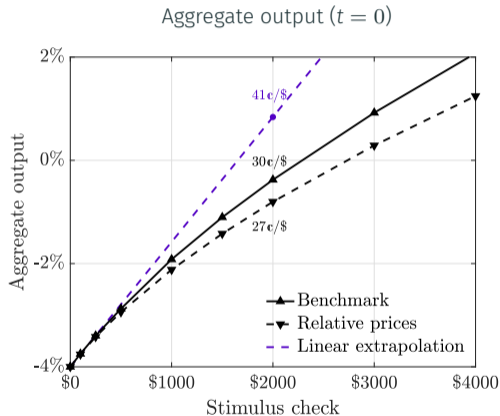


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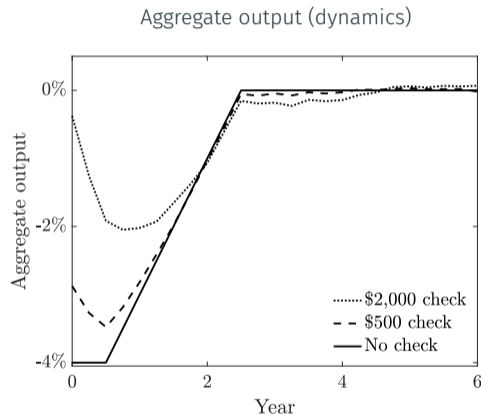
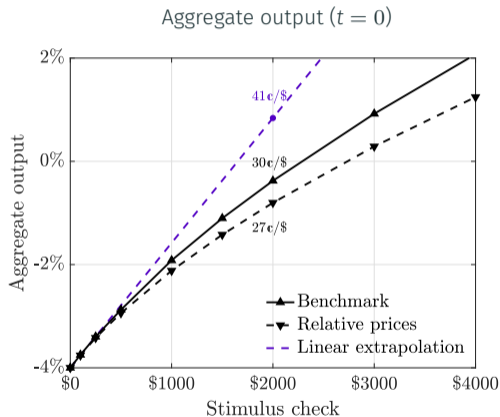
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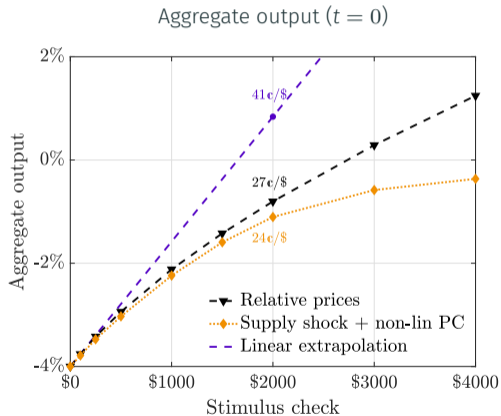


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- ▶ Perfect storm: shocks to **potential output**, non-linear NKPC

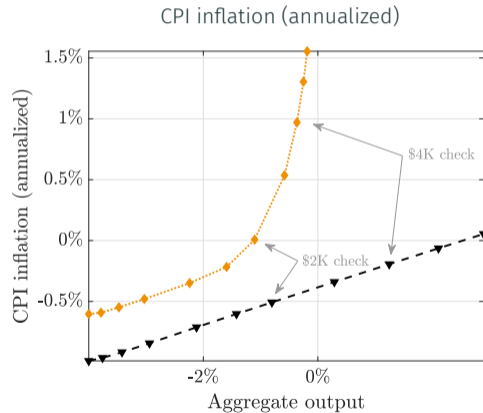
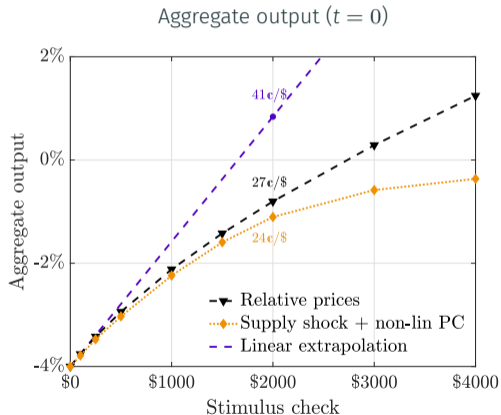
SUPPLY SIDE EFFECTS

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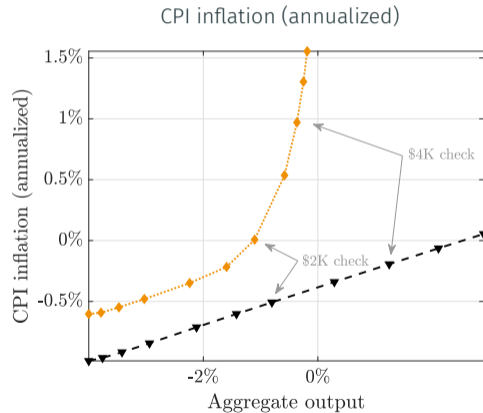
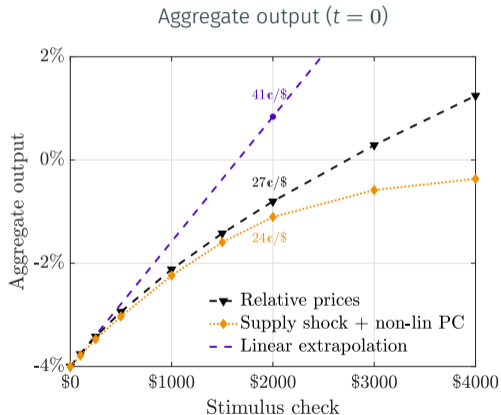
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Takeaways

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3. We embed this demand block in a **HANK model** → effect of stimulus checks?

Takeaways

1. The **MPX declines slowly** with the size of stimulus checks
2. **Larger checks remain effective** at stimulating output in recessions, but **extrapolating from small checks overestimates** their impact

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- ▶ Credit tracks d_t : households repay at the rate at which durable depreciates.
- ▶ Empirically, typical car loan is 5-6 years while car depreciates at 20%, pre-determined payments (Argyle et al.), and prepayments are rare for consumer durables (Heitfield-Sabarwal), and households make minimum down payment (Green et al.).

RECURSIVE FORMULATION

- ▶ Discrete choice problem

$$\mathcal{V}_t(\mathbf{x}; \epsilon) = \max \left\{ V_t^{\text{adjust}}(\mathbf{x}) - \epsilon, V_t^{\text{non}}(\mathbf{x}) \right\}$$

- ▶ When adjusting

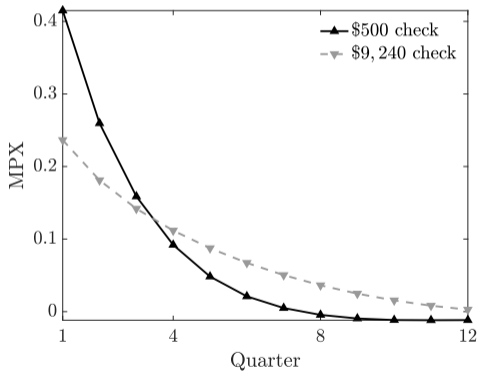
$$\begin{aligned} V_t^{\text{adjust}}(\mathbf{x}) &= \max_{c, d', m'} u(c, d') + \beta \int \mathcal{V}_{t+1}(d', m', y'; \epsilon') d\mathcal{E}(\epsilon') \Gamma(dy'; y) \\ \text{s.t. } & [1 - (1 - \theta)(1 - \delta)] d' + m' + c \leq \mathcal{Y}_t(\mathbf{x}; T_t) + \theta(1 - \delta) d \\ & m' \geq 0, \end{aligned}$$

- ▶ When not adjusting

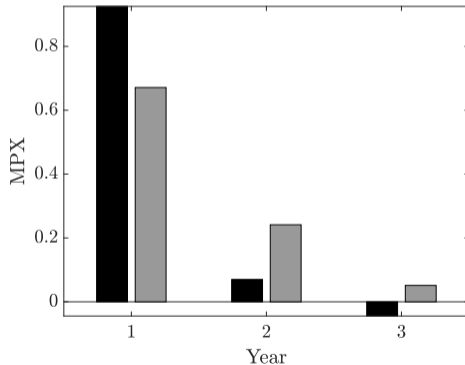
$$\begin{aligned} V_t^{\text{non}}(\mathbf{x}) &= \max_{c, m'} u(c, d') + \beta \int \mathcal{V}_{t+1}(d', m', y'; \epsilon') dG(\epsilon') \Gamma(dy'; y) \\ \text{s.t. } & m' + c \leq \mathcal{Y}_t(\mathbf{x}; T_t) - \iota\delta d - (1 - \theta)[(1 - \delta)d - d'] \\ & m' \geq 0 \end{aligned}$$

3. ANNUAL MPX

Quarterly MPX

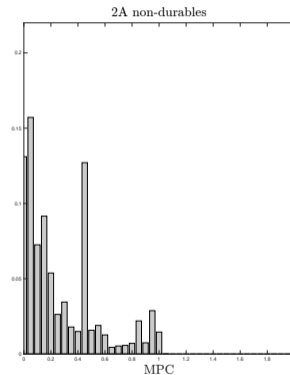
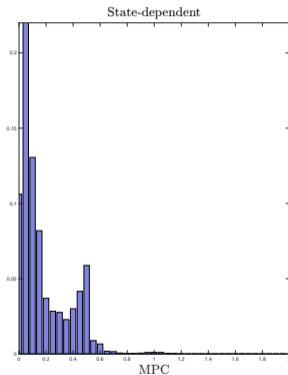
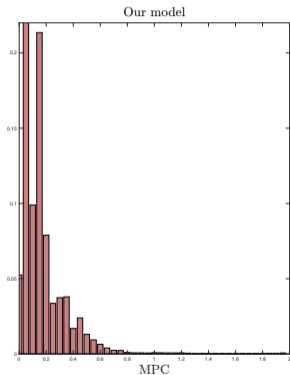


Annual MPX



4. DISTRIBUTION OF MPXS (500\$ CHECK)

- ▶ Empirically, distribution declines smoothly and large MPX (> 1) (Lewis et al., Fuster et al.)



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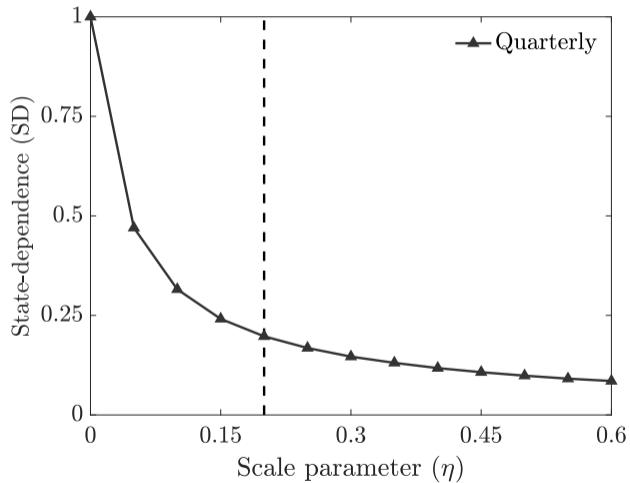
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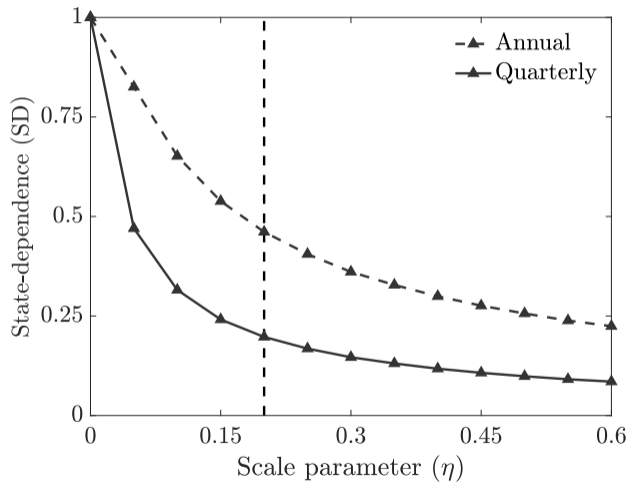
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- ▶ By definition, $SD = 1$ in state-dependent model and $SD = 0$ in Calvo model.

STATE- AND TIME-DEPENDENT ADJUSTMENTS

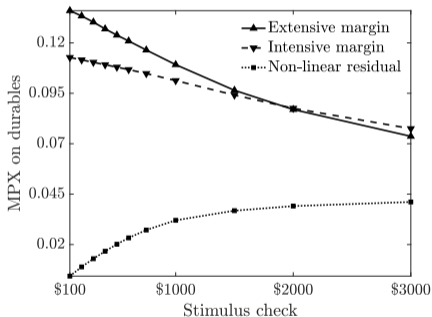


STATE- AND TIME-DEPENDENT ADJUSTMENTS



EXTENSIVE AND INTENSIVE MARGINS

- ▶ Why does the MPX ↓ in our model? Smooth hazard dampens the **extensive margin**.



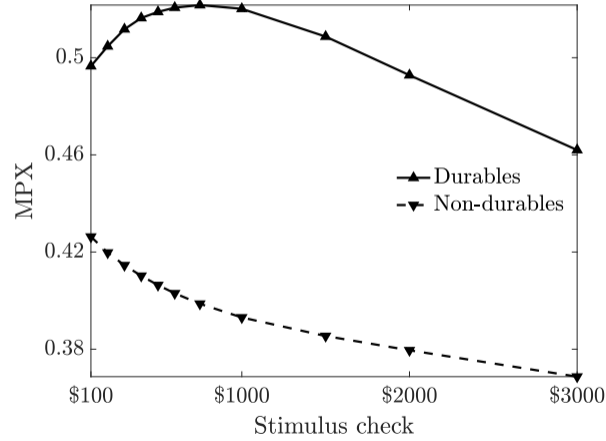
Extensive margin

$$\frac{\int \overbrace{\{\mathcal{S}_0(d, m + T, y) - \mathcal{S}_0(d, m, y)\}}^{\text{\# of marginal adjusters}} \times \overbrace{x(d, m, y)}^{\text{selection}} \times d\pi(x)}{T}$$

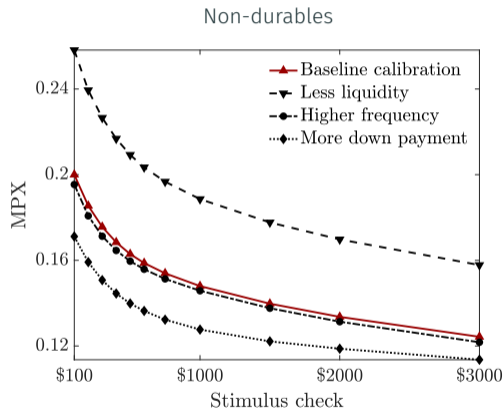
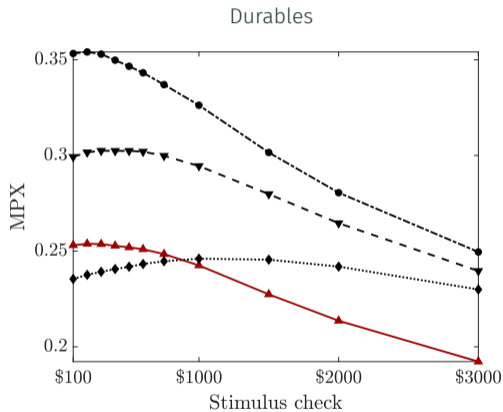
- ▶ Extensive margin \simeq Intensive margin
- ▶ **Selection** dominates (car \rightsquigarrow fridge)
- ▶ Contrasts with purely state-dep. model

SIZE-DEPENDENCE (ANNUAL MPX)

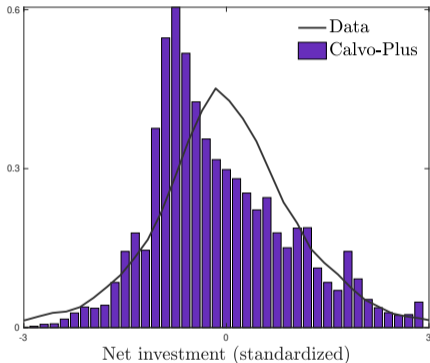
Figure 9: Annual MPX



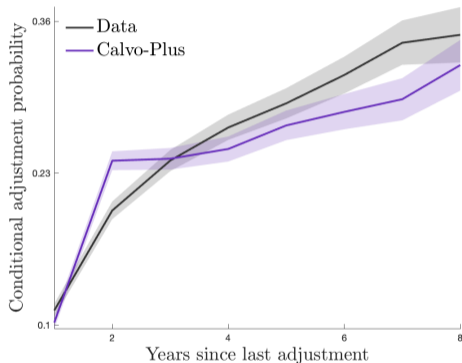
SENSITIVITY



Distribution of Investments

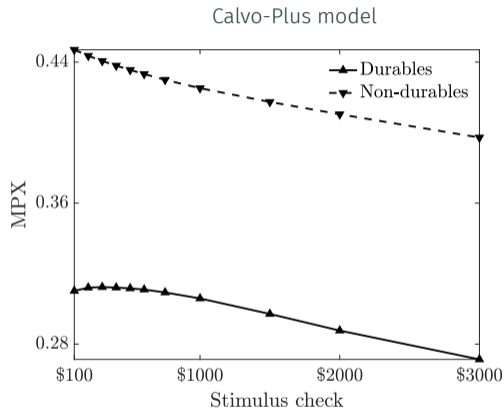
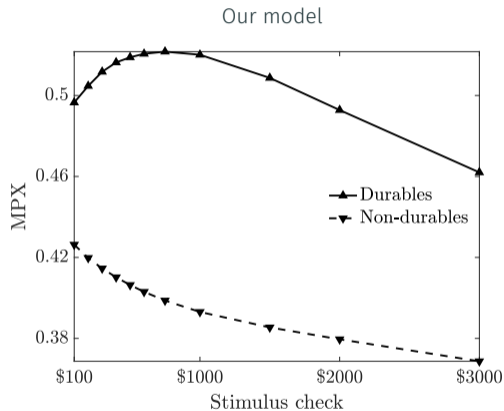


Conditional Adi. Probability



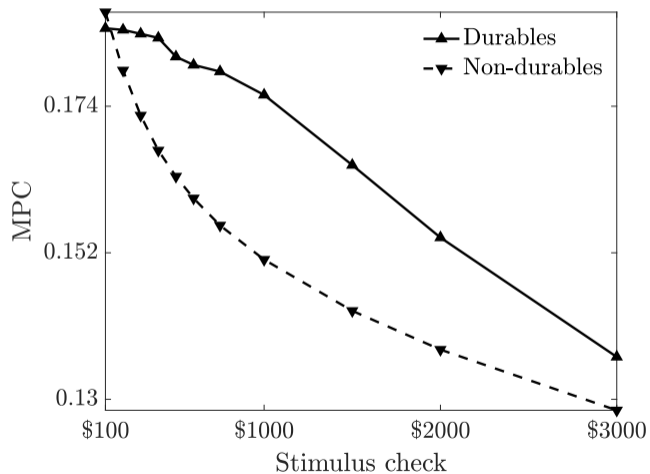
- ▶ MPX on durables (18%) is smaller than in our model (25%) and Orchard et al. (30%)
- ▶ MPX on durables and non-durables \sim same vs. our model + data (ratio 150%)

CALVO PLUS: ANNUAL MPX

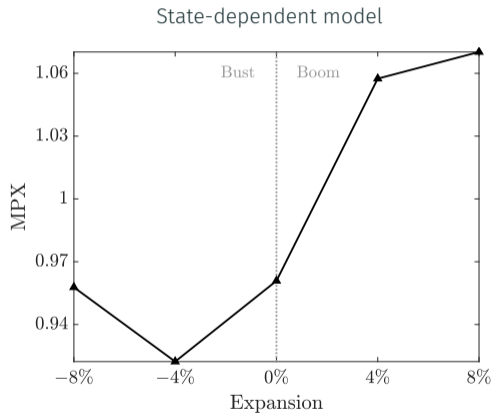
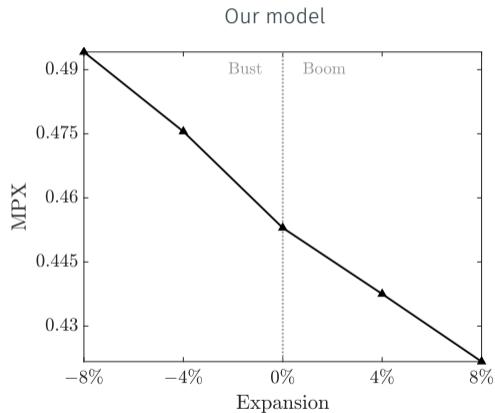


- ▶ The proportions are reversed compared to our model that matches the data!

CALVO PLUS: SIZE-DEPENDENCE



STATE-CONTINGENCY IN THE MPX



Monetary policy

$$r_t^m = \max \left\{ r^m + \phi_\pi \pi_t + \phi_y \hat{Y}_t, \underline{r} \right\}$$

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$$B_t^g = \frac{1 + r_t}{1 + \pi_t} B_{t-1}^g + \mathcal{T}_t - t_t - G_t$$

(checks t_0 financed over 15 years)

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Market clearing

$$P_t^c (C_t + G_t) + F^{-1} (X_t^{\text{dom}}) + NX_t^{\text{c,real}} = Y_t^{\text{dom}}$$

$$P_t^d X_t + p_t^d I_t + NX_t^{\text{d,real}} = p_t^d (X_t^{\text{dom}} + A_1 K_{t-1})$$

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Incomes

$$E_t^{\text{net}}(\mathbf{x}) = \psi_{0,t} \{y(Y_t + \text{Div}_t)\}^{1-\psi_1}$$

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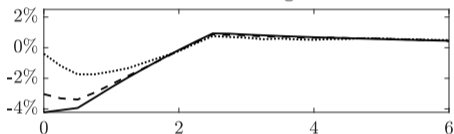
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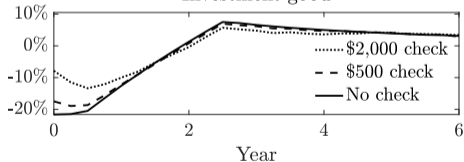
ADDITIONAL RESULTS

Sectoral output gaps

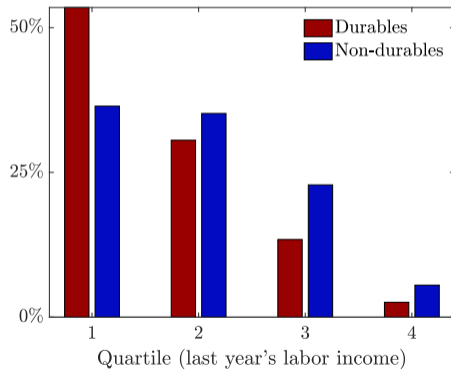
Non-durable good



Investment good



Decomposing households' responses (\$500)



1. Non-linear Phillips curve

$$\pi_t = \kappa \hat{y}_t + \kappa^* \max \{ \hat{y}_t, 0 \}^2 + \beta \pi_{t+1}$$

with $\kappa = 0.0031$ (Hazell et al.) and $\kappa^* = 0.1$ (Mavroeidis et al., Cerrato-Gitti)

2. Reduction in Y_t^{potent} and X_t^{potent} by 50% of initial gap

3. Relative price movements

$$p_t^d \equiv \left(\frac{X_t^{\text{dom}}}{X_t^{\text{potent}}} \right)^{1/\zeta}$$

with $\zeta = 1/0.049$ (McKay-Wieland)